Classification and Representation Joint Learning via Deep Networks

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Abstract

Deep learning has been proven to be effective for classification problems. However, the majority of previous works trained classifiers by considering only class label information and ignoring the local information from the spatial distribution of training samples. In this paper, we propose a deep learning framework that considers both class label information and local spatial distribution information between training samples. A two-channel network with shared weights is used to measure the local distribution. The classification performance can be improved with more detailed information provided by the local distribution, particularly when the training samples are insufficient. Additionally, the class label information can help to learn better feature representations compared with other feature learning methods that use only local distribution information between samples. The local distribution constraint between sample pairs can also be viewed as a regularization of the network, which can efficiently prevent the overfitting problem. Extensive experiments are conducted on several benchmark image classification datasets, and the results demonstrate the effectiveness of our proposed method.

1 Introduction

Classification is one important branch of machine learning. Various machine learning algorithms have been proposed to improve the classification performance, e.g., support vector machines (SVMs) [Suykens and Vandewalle, 1999; Vapnik and Vapnik, 1998], random forest [Breiman, 2001], and Bayes [Russell et al., 1995]. However, the classification performance is limited by the feature representation used for the classifier. Some hand-crafted features, such as SIFT [Lowe, 2004] and HOG [Dalal and Triggs, 2005], have been proposed to address this issue. Unfortunately, the capacity of hand-crafted features is still unsatisfactory. In recent years, deep learning has achieved excellent classification performance on various applications with a strong feature representation learning ability, such as MNIST [LeCun et al., 1998], CIFAR [Krizhevsky and Hinton, 2009], and even the

Figure 1: Illustration of the network architecture. The network used in this paper has two channels with shared weights. Two softmax losses are followed separately on top of the two channels, and our proposed pairwise loss is added to one particular layer as a regularization of the local distribution. Randomly selected pairs are fed into the network, and the parameters are updated.

large-scale dataset ImageNet [Krizhevsky et al., 2012]. Previous deep classification networks trained classification models by only utilizing the class labels of training data, measured by the softmax loss on the output layer. They ignored the local distribution information between training samples. Softmax loss focuses on whether one training sample is correctly classified. However, the local distribution between samples can provide more information. For example, similar training samples should have similar high-level feature representations, whereas the feature representations of dissimilar samples should differ from each other.

Considering this problem, we propose a pairwise loss between similar and dissimilar sample pairs to constrain the network for improving the classification performance.
Specifically, we construct a two-channel network with shared weights, and each network has its own softmax loss, which is shown in Figure 1. The proposed pairwise loss is added to one particular layer as a constraint of the learned feature representation. With this pairwise feature representation constraint, the classification performance can be improved. We will show that the contrastive loss used in the siamese network [Hadsell et al., 2006] is a special case of the proposed pairwise loss. The constraint of contrastive loss is too strong and thus may be unsuitable for real-world problems.

Pairwise constraints between samples are generally used to learn a distance metric. Distance metric learning has been applied to many machine learning problems, such as classification [Weinberger et al., 2006; Jin et al., 2009], clustering [Yeung and Chang, 2007], and retrieval [Hoi et al., 2010]. It aims to learn a transformation of the original feature, after which the distance between samples can be better estimated. However, the performance of distance metric learning is restricted due to the limitation of the feature representation and the ability of transformation. Considering its ability to learn high-level feature representations, deep learning has been used for distance metric learning. Hadsell et al. proposed a two-channel network (siamese network) with a contrastive loss for dimensionality reduction by learning an invariant mapping [Hadsell et al., 2006]. It relies solely on the neighborhood relationship to form the pairwise constraints. Considering the success of the siamese network, several works have followed this network architecture and also adopted the contrastive loss to address related problems. For example, Hyun et al. proposed a deep metric learning using lifted structured feature embedding [Oh Song et al., 2016]. Zagoruyko and Komodakis used a two-channel network to compare the similarity between image patches [Zagoruyko and Komodakis, 2015]. Sun et al. proposed a similar network architecture to learn face recognition neural networks [Sun et al., 2015]. This paper also reported that the loss of identification (classification) helped to improve the feature learning for verification. However, it did not discuss how the feature learning affected the classification performance. Similar to pairwise constraints, some deep metric learning methods use triplets as constraints to learn high-level feature representations [Cheng et al., 2016; Schroff et al., 2015; Hoffer and Ailon, 2015]. All these metric learning works focus on the neighborhood relationship and ignore the information directly provided by the class labels, which means that the procedure of composing similar or dissimilar pairs using labels may cause the loss of useful information. In this paper, we use the softmax loss to improve the performance of feature representation.

Overfitting is always a large issue in the training of deep architectures, particularly when the number of training samples is insufficient. Our proposed two-channel network can effectively prevent the overfitting problem and achieve promising results when the number of training samples is small. The reason is that the proposed pairwise loss can be viewed as a regularization of the network, which prevents the model from focusing on the label information too much. This will be demonstrated in the experiments.

The remainder of this paper is organized as follows. In Section 2, we present a detailed introduction to our proposed pairwise loss and the proposed two-channel joint learning network. Section 3 reports and analyzes various experimental results to demonstrate the effectiveness of our proposed method. Conclusions are presented in Section 4.

2 Classification and Representation Joint Learning

In this section, we provide a detailed introduction to our proposed joint learning of classification and representation. We first introduce the proposed pairwise loss and perform a comparison between our proposed pairwise loss and the commonly used contrastive loss. Then, the network architecture of combining classification and local distribution information is introduced. The stochastic gradient decent method is used to update the parameters of the network, and the updating algorithm is provided at the end of this section.

2.1 Proposed Pairwise Constraints

In this paper, the neighborhood relationships between sample pairs are used to obtain the local distribution information. Suppose that $x_i$ and $x_j$ are two input training samples in a $d$-dimensional feature space $\mathbb{R}^d$. $Y_{ij}$ indicates the similarity between $x_i$ and $x_j$, and it is defined as

$$Y_{ij} = \begin{cases} 1, & x_i \text{ and } x_j \text{ are similar;} \\ -1, & x_i \text{ and } x_j \text{ are dissimilar.} \end{cases}$$

We can obtain the similarity between samples through class labels: two samples that have the same class label are similar, and two samples that have different class labels are dissimilar. Denote the square of the Euclidean distance between $x_i$ and $x_j$ on the output manifold as follows:

$$D_k^2(x_i, x_j, \theta) = \| f_k(x_i | \theta) - f_k(x_j | \theta) \|^2_2, \quad (1)$$

where $f_k(x_i | \theta)$ indicates the output of the network on the $k$-th layer under parameters $\theta$ with input $x_i$.

The main idea of the local distribution constraint is to learn a nonlinear mapping that maps similar input vectors to nearby points and dissimilar ones to distant points on the output manifold. Previous deep metric learning methods mainly used contrastive loss to achieve this goal. In this paper, we propose a pairwise loss that is motivated mainly by regularized distance metric learning [Jin et al., 2009]. Our proposed pairwise loss is more flexible than contrastive loss, which can be viewed as a special case of our pairwise loss. The explicit loss function can be formulated as follows:

$$PLoss(x_i, x_j, \theta, k) = \max(0, b - Y_{ij}(m - D_k^2(x_i, x_j, \theta))), \quad (2)$$

where $b$ and $m$ are two parameters and $0 < b < m$. Our proposed loss can guarantee that samples belonging to the same class are clustered and that the distance between dissimilar pairs is larger than the distance between similar pairs plus a margin. For a better understanding of the loss, it can be reformulated as follows:

$$PLoss(x_i, x_j, \theta, k) = \frac{Y_{ij} + 1}{2} \max(0, b - m + D_k^2(x_i, x_j, \theta)) + \frac{1 - Y_{ij}}{2} \max(0, b + m - D_k^2(x_i, x_j, \theta)). \quad (3)$$
The contrastive loss of the siamese network can be viewed as a special case when setting the parameters of our pairwise loss as \( b = m \) and \( m = \frac{m_c}{2} \), i.e.,

\[
P_{Loss}(x_i, x_j, \theta, k) = \frac{Y_{ij} + 1}{2} \max(0, D^2_k(x_i, x_j, \theta)) \\
+ \frac{1 - Y_{ij}}{2} \max(0, 2m - D^2_k(x_i, x_j, \theta)) \\
= \frac{Y_{ij} + 1}{2} D^2_k(x_i, x_j, \theta) \\
+ \frac{1 - Y_{ij}}{2} \max(0, m_c - D^2_k(x_i, x_j, \theta)),
\]

where \( m_c \) is the margin of the contrastive loss function. The contrastive loss penalizes all similar pairs with a distance larger than zero. This constraint is too strong. It is more reasonable that the distance between similar pairs is a range within a margin rather than being zero. The comparison between our proposed pairwise loss and the contrastive loss is presented in Figure 2. In this figure, there are two classes of training samples, three blue circles and two green squares. In the original feature space, the distance between the samples in the same classes is larger than the distance between samples from different classes. After the training with our pairwise loss, the distance between similar pairs will be smaller than a margin \( m - b \), and the distance between dissimilar pairs will be larger than \( m + b \). For contrastive loss, it is a special case of pairwise loss when \( b = m \). In this case, the distance between similar pairs is constrained to be zero, which is too strong for real-world problems.

\[L = \frac{2}{N(N-1)} \sum_{i,j=1}^{N} (C_{Loss}(x^i, W_1, y_i) \\
+ C_{Loss}(x^j, W_1, y_j) + \lambda P_{Loss}(x_i, x_j, \theta, k)),\]

where \( \lambda > 0 \) is one trade-off parameter. \( W_1 \) and \( W_2 \) are parameters of the two softmax losses. The two softmax losses have the same loss weight to guarantee the symmetry of the network. If only one softmax is added or the loss weights are different, then the two samples of the input pairs are treated unfairly, which may lead to a decrease in the performance. For softmax loss, the pairwise loss can be viewed as a regularization on the feature representation using local distribution information. It can be viewed as an indirect regularization on the parameters of the network. Consequently, it can prevent the network from overfitting. Furthermore, the local distribution information can also help improve the classification performance by providing more specific local distribution information. Additionally, it is slow and difficult for our proposed pairwise loss or contrastive loss to converge to a promising solution with random selection of training pairs. There are mainly two reasons. First, feeding all training pairs into the network requires too much time because of the large amount

deleted words
of possible pairs. Second, the learning rate used for the pairwise loss is generally small. However, the softmax loss does not have such drawbacks, which can help the pairwise loss converge faster and obtain a better solution. Consequently, the performance of feature representation can be improved.

We use the stochastic gradient decent method to update the parameters of the network. The learning algorithm is presented in Algorithm 1.

### 3 Experiments

To evaluate the effectiveness of our proposed method, we conduct various experiments on three benchmark datasets: MNIST, SVHN, and CIFAR10. All experiments are implemented using the CAFFE deep learning framework [Jia et al., 2014]. The first dataset used in our experiment is MNIST, which consists of a training set of 60000 28 × 28 handwritten digits of 10 classes and a test set of 10000 samples. The second dataset is the Street View House Numbers (SVHN), which consists of over 600000 32 × 32 color images of house number digits 0-9. This dataset is split into 73257 digits for training, 26032 digits for testing, and 531311 extra training digits that are less difficult to recognize. Note that the extra training digits are not used in any experiment in this paper. The third dataset used in our experiment is CIFAR10, which consists of 60000 32 × 32 color images from 10 classes. This dataset is split into 50000 training samples and 10000 test samples.

We compare our proposed method with several baselines. The first is the siamese network (siamese) with contrastive loss. The architecture of the siamese network is also a two-channel network but with only contrastive loss. The second is our pairwise loss (pairloss), which is supposed to have better performance than the siamese network. In the experiments, we randomly sample two batches of training samples into the two branches of the network and use the contrastive loss or pairwise loss on the top. The purpose of these two methods is to learn a high-level feature representation using pairwise constraints, and then a classifier (KNN or SVM) is applied on these features. The third method is to use softmax loss to improve the performance of pairwise loss (pair-soft). This will demonstrate that classification loss can derive better feature representation learning. The fourth method is the normal single-channel network with a softmax layer on the top to perform classification (singlenet). The final method is to combine the pairwise loss with softmax loss to improve the classification performance (pairnet), which will demonstrate that the local distribution information can provide more specific information than only using labels directly. The specific layer and parameter settings for each dataset are introduced in their own experiments.

#### 3.1 MNIST Dataset

In this section, we present experimental details and the results on MNIST datasets. We use LeNet to conduct all experiments on MNIST. LeNet consists of 2 convolutional layers, and both of these layers are followed by a 2 × 2 max-pooling layers. Then, two fully connected layers are followed. The only preprocessing of the data is a global normalization that normalizes the pixel values of the image to 0-1. To train the models, we randomly select different numbers (60, 100, 500, and 1000 samples for each class) of training samples from the training set. We also train the model by using all training samples in the training set (denoted as “ALL”). All random selections are repeated three times to avoid randomness. A KNN classifier is applied on the learned features via contrastive loss, pairwise loss and pair-soft loss. The experimental results are summarized in Table 1.

From the results in Table 1, we can conclude that our pairwise loss outperforms the contrastive loss with different amounts of training samples. Comparing the results between pairloss and pair-soft, it is clear that the softmax loss helps to improve the performance of the pairwise loss, which means that a better feature representation is learned. The pairnet performs considerably better than singlenet, particularly when the number of training samples is small, which demonstrates the effectiveness of the combination of pairwise loss and softmax loss. When the number of training samples is small, the information provided directly by the class label is limited. However, the pairwise constraints can provide more information about the feature distribution, leading to better classification performance.

We conduct another experiment to verify the feature rep-
representation learning ability of our proposed pairwise loss and analyze the effects of the parameters by visualizing the features in 2-D space. We add another fully connected layer on top of the network and set the output dimensionality as 2. The pairwise loss is used to learn feature representations by setting the parameter \( b \) to 0, 0.5, and 1. The final results are shown in Figure 3. Each of the sub-figures has 10 clusters corresponding to digits 0-9. In the illustration of Figure 2, we can observe that when the parameter \( b \) is set to smaller values, the circle that constrains the similar pairs will be larger. This result means that the size of the clusters is larger. From the results presented in Figure 3, we can observe that the size of the cluster decreases with the value of parameter \( b \) varying from 0-1. When the value of \( b \) is set to 1, which is equal to parameter \( m \), this can be viewed as contrastive loss used in the siamese network.

### 3.2 SVHN Dataset

In this section, we conduct experiments on the SVHN dataset. The network architecture used for the SVHN dataset consists of 3 convolutional layers, and each of them is followed by a max-pooling layer. ReLU non-linearity is applied between two convolutional layers. Two fully connected layers are added after the convolutional layers. Note that the extra training dataset is not used in our experiments. We preprocess the images using local contrast normalization [Zeiler and Fergus, 2013] due to the large variety of colors and brightness variations in the images. After the local contrast normalization, we crop the image into a 28 \( \times \) 28 patch that is located in the center of the image. No data augmentation is applied in our experiments. To train the models, we randomly select different numbers (2000 and 500 samples for each class) of training samples from the training set. We also train the model by using all training samples in the training set (denoted as “ALL”). All random procedures are repeated three times, and the average performance is reported to avoid randomness. A KNN classifier is applied on the learned features. The results are shown in Table 2.

From Table 2, we can obtain conclusions similar to those from the experiments on the MNIST dataset. The pairwise loss and the softmax loss help to improve the performance of each other consistently. The improvement is particularly obvious when the amount of training samples is small. Additionally, we present results to demonstrate the ability of our proposed method to prevent overfitting in Figure 4 and Figure 5. We randomly select 500 samples from each class and use the same network as used in the above experiments on SVHN. We compare the proposed pairnet with singlenet to verify its ability to prevent overfitting. Note that the same weight decay is used for these two networks. From Figure 4 and Figure 5,

### Table 1: Classification performance on MNIST dataset corresponding to different amounts of training samples.

<table>
<thead>
<tr>
<th>Methods</th>
<th>ALL</th>
<th>10000</th>
<th>5000</th>
<th>1000</th>
<th>600</th>
</tr>
</thead>
<tbody>
<tr>
<td>siamese</td>
<td>0.9731</td>
<td>0.9715 ± 0.0017</td>
<td>0.9674 ± 0.0026</td>
<td>0.9379 ± 0.0054</td>
<td>0.9171 ± 0.0029</td>
</tr>
<tr>
<td>pairloss</td>
<td>0.9795</td>
<td>0.9791 ± 0.0003</td>
<td>0.9753 ± 0.0022</td>
<td>0.9432 ± 0.0062</td>
<td>0.9257 ± 0.0043</td>
</tr>
<tr>
<td>pair-soft</td>
<td>0.9908</td>
<td>0.9864 ± 0.0007</td>
<td>0.9824 ± 0.0008</td>
<td>0.9630 ± 0.0044</td>
<td>0.9517 ± 0.0037</td>
</tr>
<tr>
<td>singlenet</td>
<td>0.9892</td>
<td>0.9820 ± 0.0022</td>
<td>0.9793 ± 0.0029</td>
<td>0.9397 ± 0.0064</td>
<td>0.9247 ± 0.0116</td>
</tr>
<tr>
<td>pairnet</td>
<td>0.9917</td>
<td>0.9875 ± 0.0007</td>
<td>0.9834 ± 0.0001</td>
<td>0.9637 ± 0.0019</td>
<td>0.9510 ± 0.0057</td>
</tr>
</tbody>
</table>

### Table 2: Classification performance on the SVHN dataset corresponding to different amounts of training samples.

<table>
<thead>
<tr>
<th>Methods</th>
<th>ALL</th>
<th>20000</th>
<th>5000</th>
</tr>
</thead>
<tbody>
<tr>
<td>siamese</td>
<td>0.8856</td>
<td>0.8730 ± 0.0010</td>
<td>0.7887 ± 0.0109</td>
</tr>
<tr>
<td>pairloss</td>
<td>0.8998</td>
<td>0.8779 ± 0.0038</td>
<td>0.8112 ± 0.0172</td>
</tr>
<tr>
<td>pair-soft</td>
<td>0.9080</td>
<td>0.8934 ± 0.0009</td>
<td>0.8552 ± 0.0010</td>
</tr>
<tr>
<td>singlenet</td>
<td>0.9219</td>
<td>0.8885 ± 0.0006</td>
<td>0.8426 ± 0.0081</td>
</tr>
<tr>
<td>pairnet</td>
<td>0.9387</td>
<td>0.9171 ± 0.0014</td>
<td>0.8876 ± 0.0010</td>
</tr>
</tbody>
</table>

### Table 3: Classification performance on the CIFAR10 dataset corresponding to different amounts of training samples.

<table>
<thead>
<tr>
<th>Methods</th>
<th>ALL</th>
<th>10000</th>
<th>5000</th>
</tr>
</thead>
<tbody>
<tr>
<td>siamese</td>
<td>0.8635</td>
<td>0.7286 ± 0.0145</td>
<td>0.6917 ± 0.0338</td>
</tr>
<tr>
<td>pairloss</td>
<td>0.8539</td>
<td>0.7430 ± 0.0075</td>
<td>0.6789 ± 0.0254</td>
</tr>
<tr>
<td>pair-soft</td>
<td>0.8774</td>
<td>0.7375 ± 0.0022</td>
<td>0.6671 ± 0.0056</td>
</tr>
<tr>
<td>singlenet</td>
<td>0.8609</td>
<td>0.7612 ± 0.0107</td>
<td>0.7055 ± 0.0002</td>
</tr>
<tr>
<td>pairnet</td>
<td>0.8697</td>
<td>0.7612 ± 0.0107</td>
<td>0.7055 ± 0.0002</td>
</tr>
</tbody>
</table>

![Figure 3: Test sample clustering results with different parameters on MNIST dataset.](image-url)
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3.3 CIFAR10 Dataset

We also conduct experiments on the CIFAR10 dataset. This dataset is more difficult than the MNIST dataset and the SVHN dataset. Consequently, the architecture of the network used for training CIFAR10 is more complex. We adopt a network similar to that used in [Hoffer and Ailon, 2015], which consists of 4 convolutional layers and 1 fully connected layer. Each of the first three convolutional layers is followed by a max-pooling layer. A ReLU layer is applied between two consecutive layers. Finally, a softmax layer is added on the top of the network for classification. The images are preprocessed by performing global contrast normalization as used for the SVHN dataset. Then, ZCA whitening is performed, which makes the pixels less correlated with each other and have the same variances [Srivastava et al., 2014]. Note that the training of the network converges slowly if we use only contrastive loss or pairwise loss, which mainly has two reasons. First, CIFAR10 is more difficult, and the network architecture is more complicated. Second, the number of pairs in our model in each batch is small due to the storage limitations of the GPU. Consequently, we do not compare the performance of contrastive loss and pairwise loss. Rather, we add a softmax loss on top of the siamese network (siamese-soft) and compare its performance with the other methods.

First, we compare the performance using all the training data and then randomly select 1000 and 500 samples from each class as the training set to compare the performance of all the methods. Each random selection is repeated three times to avoid randomness. The results are shown in Table 3.

Note that SVM is used to classify the learned features of siamese-soft and pair-soft. From the results presented in Table 3, we can conclude that our proposed pairnet outperforms the other methods. The contrastive loss and pairwise loss converge faster through training with a softmax loss, and both of the methods can obtain performance comparable to that of singlenet.

4 Conclusions

In this paper, we propose a deep network architecture to learn classification and feature representation simultaneously, which can enhance the performance of each other. A pairwise loss is proposed to constrain the feature representation learning. Then, we propose a two-channel network with the proposed pairwise loss as a regularization of the feature distribution. The classification performance can be improved with this regularization. Additionally, the softmax loss used in classification can also help to learn better feature representations. The pairwise loss can be viewed as an indirect regularization on the weights of the network, which prevents overfitting when the training samples are insufficient. Extensive experiments are conducted on three benchmark datasets, and the experimental results demonstrate the effectiveness of our proposed method.

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